

# Reducibility, Thermal and Mass Scaling in Angular Correlations from Multifragmentation Reactions

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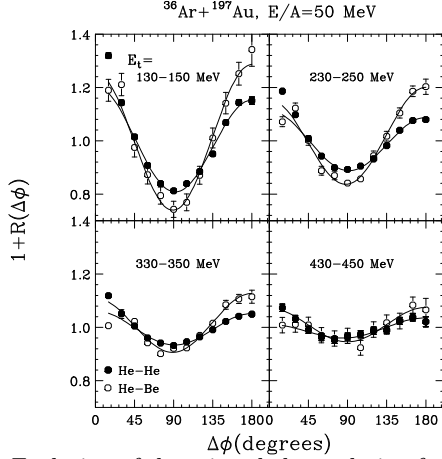


FIG. 1. Evolution of the azimuthal correlation functions of two He particles (solid circles) and He and Be particles (open circles) emitted at  $\theta_{lab} = 31^\circ$ - $50^\circ$  for four different cuts on the transverse energy  $E_t$ . The solid lines are fits described in ref. [1].

We have explored the azimuthal correlations between emitted particles to search for thermal scaling of the correlation amplitudes and reducibility of the two-fold emission probability to that of the one-fold [1]. Fig. 1 shows azimuthal correlation functions of different particle pairs for different values of the transverse energy  $E_t$ . Consistent with previous observations, the azimuthal correlation functions exhibit a slightly distorted V-shape pattern. At larger excitation energies (assumed proportional to  $E_t$ ) the correlations become progressively damped.

To understand the evolution of the correlation functions of Fig. 1, we have considered the exactly solvable problem of thermal particle emission from a rotating source. The classical probability of emitting a particle with reduced mass  $\mu$  from the surface of a rotating system (of angular momentum  $I$ , moment of inertia  $\mathfrak{I}$ , temperature  $T$  and distance  $R$  between centers of the “daughter” and emitted nuclei) in a direction given by polar angle  $\theta$  (in the center of mass frame) and azimuthal angle  $\phi$  (measured with respect to the reaction plane) is:

$$P(\theta, \phi) \propto \exp \left[ -\beta \sin^2 \theta \sin^2 \phi \right] \quad (1)$$

where

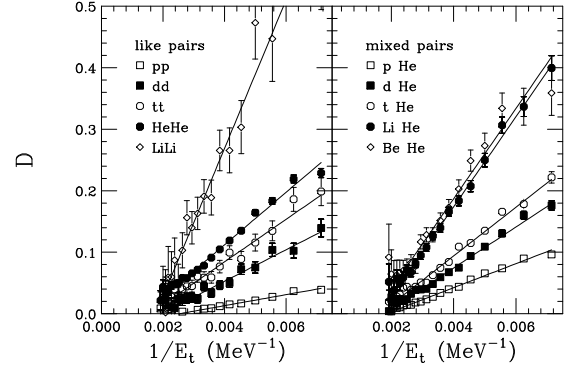


FIG. 2. Left panel: The fit parameter  $D$  as a function of  $1/E_t (\propto 1/T^2)$  for the indicated identical particle pairs. Solid lines are linear fits to the data. Right panel: Same as left panel but for particle pairs of different masses.

$$\beta = \frac{\hbar^2 I^2}{2\mathfrak{I}T} \frac{\mu R^2}{(\mathfrak{I} + \mu R^2)} = \frac{E_{rot}}{T} \frac{\mu R^2}{(\mathfrak{I} + \mu R^2)} \quad (2)$$

and  $E_{rot}$  is the rotational energy of the source.

If the fragments are emitted independently of one another, the joint probability of observing two particles at a given polar angle  $\theta$  and different azimuthal angles  $\phi$  and  $\phi + \Delta\phi$  is  $P(\theta, \phi, \Delta\phi) = P(\theta, \phi)P(\theta, \phi + \Delta\phi)$ . The resulting probability distribution must be averaged over the different directions of  $\vec{l}$  arising from different orientations of the impact vector and one obtains proportionality to a modified Bessel function of zeroth order. Expanding this function, the joint probability is approximately:

$$P(\theta, \Delta\phi) \propto 1 + \frac{D}{1 + D/2} \cos 2\Delta\phi + \frac{D^2}{(D + 2)^2} \cos^2 2\Delta\phi \quad (3)$$

where  $D = (\beta^2 \sin^4 \theta)/8 \propto 1/T^2 \propto 1/E_t$ .

A plot of  $D$  (extracted from fits to the correlation data, see Fig. 1) as a function of  $1/E_t$  is given in Fig. 2. The simplest explanation for the observed linear behavior (thermal scaling) is that the fragmenting system attains an average rotational energy which is largely independent of  $E_t$ .

[1] L. Phair et al., Phys. Rev. Lett. **77**, 822 (1996).